

Section 4.3

- 1) Consider the region bounded by the graph of $f(x) = \sqrt[3]{x}$, the x -axis, the y -axis, and the line $x = 1$. Evaluate the limit

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n f(c_i) \Delta x_i$$

where c_i is the right endpoint of the partition given by $c_i = \frac{i^3}{n^3}$, and Δx_i is the width of the i th interval.

- 2) Evaluate the definite integral $\int_2^6 5x \, dx$ using the limit process.

3) Sketch the region corresponding to each definite integral. Then evaluate each integral using a geometric formula.

a) $\int_3^5 2 \, dx$

b) $\int_1^4 (x - 1) \, dx$

c) $\int_0^4 \sqrt{16 - x^2} \, dx$

4) Find the following:

a) $\int_{\pi/2}^{\pi/2} \cos x \, dx$

b) $\int_4^1 (x - 1) \, dx$

c) $\int_0^2 |x - 1| \, dx$

5) Assuming $\int_0^2 x^3 \, dx = 4$, $\int_0^2 3x \, dx = 6$, and $\int_0^2 5 \, dx = 10$, find

$$\int_0^2 \left(\frac{1}{3}x^3 + 3x - 5 \right) dx$$